

# The Statistical Cost of Robust Kernel Hyperparameter Turning

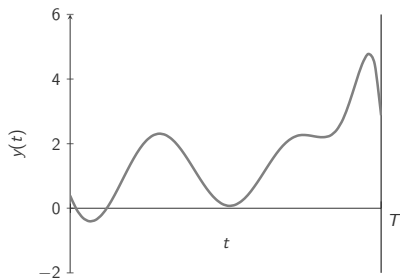
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Raphael A. Meyer with Christopher Musco

NYU, Tandon School of Engineering

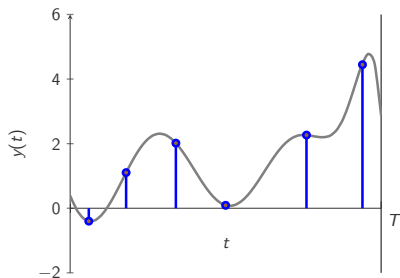


# Robust Active Interpolation



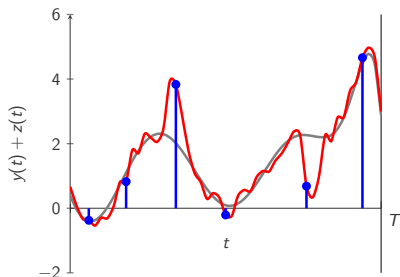
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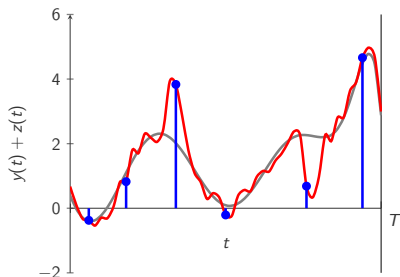
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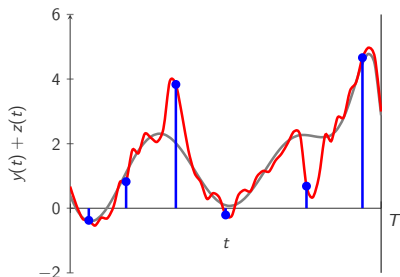
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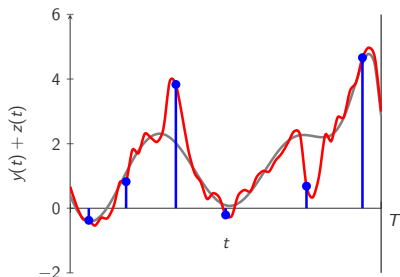
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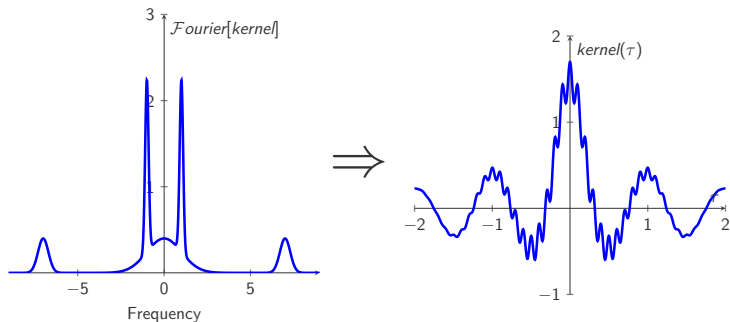
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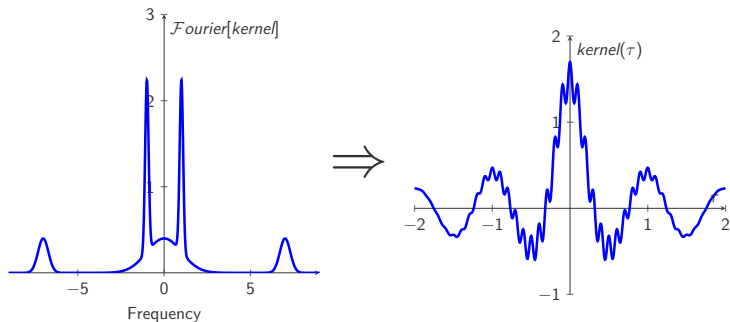
# Spectral Mixture Kernel



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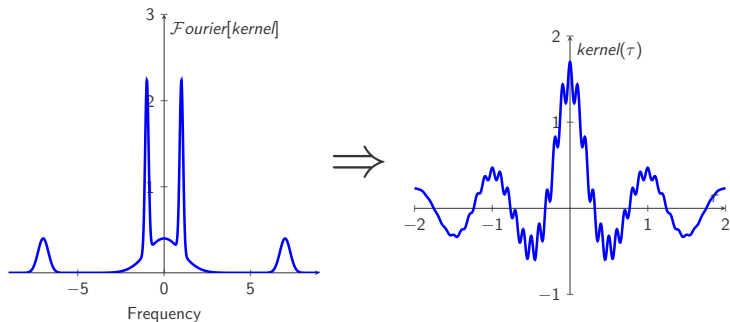


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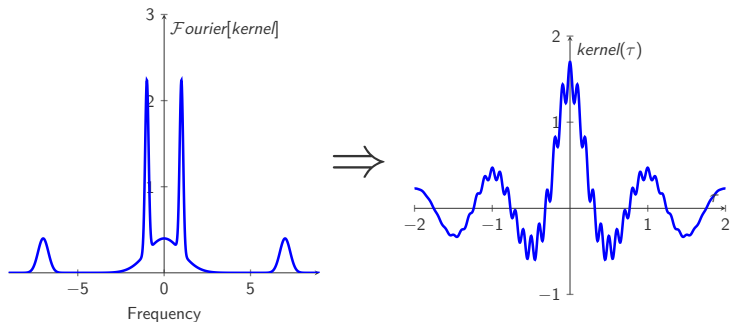
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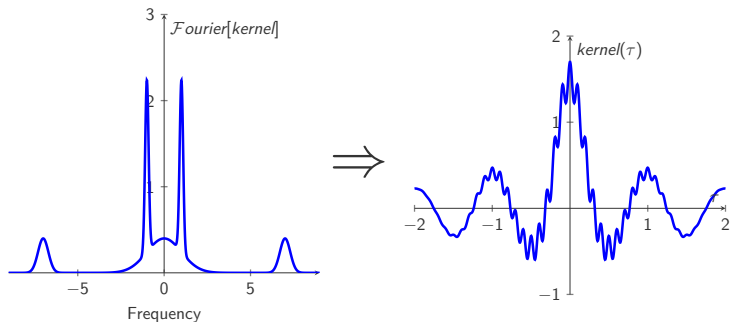
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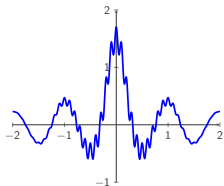
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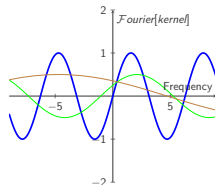
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  - Is this because we need new algorithms?

# Our Core Contribution

## Kernel Ridge Regression



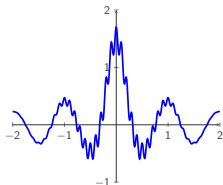
## Sparse Fourier Fitting



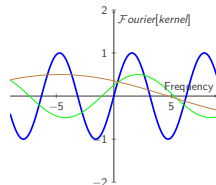
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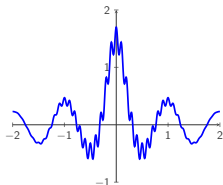
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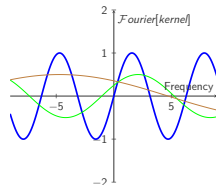
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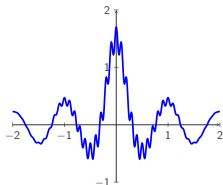
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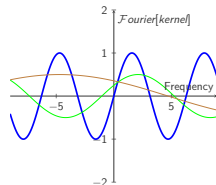
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- ⊙ Reduce Kernel Learning to a Sparse Fourier Fitting problem
- ⊙ Number of Observations needed for learning a Spectral Mixture Kernel with  $Q$  Gaussians is  $\tilde{O}(Q^2)$
- ⊙ Learning Spectral Mixture kernels is not statistically difficult
- ⊙ Techniques generalize to other Stationary Kernels



Thank You!

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Andrew Wilson and Ryan Adams.

Gaussian process kernels for pattern discovery and extrapolation.

In International Conference on Machine Learning, pages 1067–1075, 2013.